

## Optimisation MODLIN

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Idée : utiliser la structure de famille et l'indépendance du calcul des vraisemblances des sous familles pour optimiser la calcul du gradient utilisé par les optimiseurs (quasi newton, gradient conjugués....). Exemple : lors d une variation infinitésimale d'une variance d'une familles d'un père ip , les autres famille de père garde la même valeur de vraisemblance.

Fonctionnement : Actuellement, on écrit une fonction de vraisemblance prenant comme paramètres :

N : le nombre de paramètre a optimiser

X : les valeurs des paramètres à tester

F : le résultat de la vraisemblance globale

sur 1 exemple de 2 familles de père accouplé avec 3 meres (2 avec le pere 1 et 1 avec le pere 2), nous avons comme interprétation de X :

Sig 1	Sig 2	MuGen	PolyPere1	PolyPere2	PolyMere1	PolyMere2	PolyMere3
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Les 4 sous familles sont influencés par les paramètres grisés (et la variation des autres paramètres n'influence pas le résultat de la vraisemblance de la famille) :

ip=1, jm=1

Sig 1	Sig 2	MuGen	PolyPere1	PolyPere2	PolyMere1	PolyMere2	PolyMere3
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ip=1, jm=2

Sig 1	Sig 2	MuGen	PolyPere1	PolyPere2	PolyMere1	PolyMere2	PolyMere3
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ip=2, jm=3

Sig 1	Sig 2	MuGen	PolyPere1	PolyPere2	PolyMere1	PolyMere2	PolyMere3
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L'idée est donc de donner à l'optimisateur :

- Un filtre de booléen (taille N) pour chaque famille IP,JM indiquant les paramètres de X influençant la vraisemblance de la famille IP-JM
- Une fonction de VRAISSEMBLANCE d'une sous famille à optimiser, générique à l'ensemble des sous famille (FUNCT(IP,JM,N,X,F)).

Note :

Cette optimisation ne peux s appliquer aux méthodes pour les données pré-calculés puisque le calcul de vraisemblance de la dernière mère à estimer est en fonction des autres mères estimables.

## Calcul du gradient

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Le calcul du gradient optimisé s 'écrit donc:

```

XP=X
POUR I=1, N
XP(I)=X(I)-H
FMOINH=0
POUR IP=1,NP
    POUR JM=1,NM
        SI ( FILTRE(IP,JM,I) ) ALORS
            FMOINH=FMOINH+FM(IP,JM) // ON RECUPERE LA DERNIERE VALEUR CALCULE
        SINON
            APPEL FUNCT(IP,JM,N,X,FTEMP)
            FMOINH=FMOINH+FTEMP
        FIN SI
    FIN POUR(JM)
FIN POUR (IP)

XP(I)=X(I)+H
FPLUSH=0
POUR IP=1,NP
    POUR JM=1,NM
        SI ( FILTRE(IP,JM,I) ) ALORS
            FPLUSH=FPLUSH+FM(IP,JM) // ON RECUPERE LA DERNIERE VALEUR CALCULE
        SINON
            APPEL FUNCT(IP,JM,N,X,FTEMP)
            FPLUSH=FPLUSH+FTEMP
        FIN SI
    FIN POUR(JM)
FIN POUR (IP)
//CALCUL DU GRADIENT POUR LE PARAMETRE I
G(I) = (FPLUSH - FMOINH) / 2*H
XP=X
FIN POUR (I)

```

## Construction du filtre

La construction du filtre se fait a partir de la matrice d'incidence réduite (l'estimabilité des paramètres via cholesky nous donne la matrice d'incidence effective utilisé lors de l'optimisation). Elle est automatique et ne nécessite pas d apriori (pas besoin de connaître les niveaux a estimer) : Pour chaque colonnes de cette matrice (correspondant au ième parametre de X), on teste si l'ensemble des valeurs est égale à zéro. Si c'est le cas, le ième paramètres de X n'influence pas la vraisemblance de la sous famille ip-jm.

```

filter=.true.
filter(:,:,1:np+1)=.false.
do ip=1,np
    filter_inc(ip,nmp(ip)+1:nmp(ip+1),ip)=.true.
    do jm=nmp(ip)+1,nmp(ip+1)
        kd1=kd2+1
        kd2=kd2+count(presentc(ic,ndm(jm)+1:ndm(jm+1)))
        filter(ip,jm,np+1:nbnivest)=any(XINCREDUIT(kd1:kd2,:nbnivest)/=0.d0
, dim=1)

        end do
    end do

```

## Benchmark

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Compilation en mode optimisé O4 avec gfortran

3 exemples sont donnés : marie damon,nicolas deschamp et exemple porc:

Chaque exemple présente :

- la taille du jeu de donnee : np,nm,effet de nuisance => nombre de niveau a estime
- 2 prints d'exécution non optimisé et optimisé , chaque ligne correspond à :
  - temps de l'optimisation
  - nombre d'appel effectif du calcul de la vraisemblance total
  - nombre d'appel au calcul de gradient
  - nombre d'appel evité du a la recuperation de la vraisemblance d'une famille
  - le taux d'appel optimisé (nb appel evité/ (nb appel + nb appel evite) )
- Le filtre initialisé sous H0 en guise d exemple (ce filtre étant recalculé à chaque position par la suite)

Voici un tableau récapitulatifs des résultats.

Exemple	Effets de nuisances	Nb niveaux(H1)	Temps cumul non optim	Temps cumul optim	Taux d'optimisation
Marie	0	53	3,34	0,40	91,70%
Nicolas	5	61	8,54	3,77	58,70%
Exemple porc	0	16	0.240	0,07	76,50%

### Exemple MARIE DAMON

9 : NP  
39 : NM  
0 : Effets de nuisances  
53 : NTNIV (H1)

\* pas optimisé \*

TEMPS UNIT | LRT | NB APPEL FUNCT Famille IP,JM | NB APPEL GRADIENT | APPEL EVITE | NB APPEL EVITE/ APPEL TOTAL | TEMPS CUMULES

0.07999992	275.059	call	funct:	3104	call	gradient:	45	avoid	call:	0	0.0%	0.080
0.24000025	254.550	call	funct:	6534	call	gradient:	54	avoid	call:	0	0.0%	0.320
0.09999990	253.013	call	funct:	2782	call	gradient:	23	avoid	call:	0	0.0%	0.420
0.15000010	252.331	call	funct:	4113	call	gradient:	34	avoid	call:	0	0.0%	0.570
0.13999987	251.533	call	funct:	3871	call	gradient:	32	avoid	call:	0	0.0%	0.710
0.12000036	250.439	call	funct:	3387	call	gradient:	28	avoid	call:	0	0.0%	0.830
0.16999960	249.627	call	funct:	4718	call	gradient:	39	avoid	call:	0	0.0%	1.000
0.12000036	249.636	call	funct:	3266	call	gradient:	27	avoid	call:	0	0.0%	1.120
0.09999990	250.406	call	funct:	2782	call	gradient:	23	avoid	call:	0	0.0%	1.220
0.05999994	252.001	call	funct:	1815	call	gradient:	15	avoid	call:	0	0.0%	1.280
0.07000017	253.554	call	funct:	2057	call	gradient:	17	avoid	call:	0	0.0%	1.350
0.08999968	253.276	call	funct:	2298	call	gradient:	19	avoid	call:	0	0.0%	1.440
0.12000036	251.231	call	funct:	3386	call	gradient:	28	avoid	call:	0	0.0%	1.560
0.19000006	250.754	call	funct:	4960	call	gradient:	41	avoid	call:	0	0.0%	1.750
0.08999968	251.502	call	funct:	2420	call	gradient:	20	avoid	call:	0	0.0%	1.840
0.11000013	252.829	call	funct:	3146	call	gradient:	26	avoid	call:	0	0.0%	1.950
0.08999968	254.301	call	funct:	2662	call	gradient:	22	avoid	call:	0	0.0%	2.040
0.12000036	255.552	call	funct:	3146	call	gradient:	26	avoid	call:	0	0.0%	2.160
0.07999992	256.075	call	funct:	2178	call	gradient:	18	avoid	call:	0	0.0%	2.240
0.10999966	255.997	call	funct:	3024	call	gradient:	25	avoid	call:	0	0.0%	2.350
0.11999989	255.540	call	funct:	3145	call	gradient:	26	avoid	call:	0	0.0%	2.470
0.17000008	255.123	call	funct:	4596	call	gradient:	38	avoid	call:	0	0.0%	2.640
0.16000032	255.112	call	funct:	4477	call	gradient:	37	avoid	call:	0	0.0%	2.800
0.16999960	255.318	call	funct:	4598	call	gradient:	38	avoid	call:	0	0.0%	2.970
0.17000008	255.524	call	funct:	4719	call	gradient:	39	avoid	call:	0	0.0%	3.140
0.19999981	255.668	call	funct:	5324	call	gradient:	44	avoid	call:	0	0.0%	3.340

\* Gradient Optimisé \*

TEMPS UNIT | LRT | NB APPEL FUNCT Famille IP,JM | NB APPEL GRADIENT | APPEL EVITE | NB APPEL EVITE/ APPEL TOTAL | TEMPS CUMULES

0.01000023	275.059	call funct:	335	call gradient:	45	avoid call:	2768	89.2%	0.010
0.01999998	254.550	call funct:	554	call gradient:	55	avoid call:	6100	91.7%	0.030
0.01000023	253.013	call funct:	231	call gradient:	23	avoid call:	2550	91.7%	0.040
0.01999998	252.331	call funct:	342	call gradient:	34	avoid call:	3770	91.7%	0.060
0.01999998	251.533	call funct:	322	call gradient:	32	avoid call:	3548	91.7%	0.080
0.01999998	250.439	call funct:	292	call gradient:	29	avoid call:	3215	91.7%	0.100
0.01999998	249.629	call funct:	322	call gradient:	32	avoid call:	3548	91.7%	0.120
0.01999998	249.635	call funct:	362	call gradient:	36	avoid call:	3991	91.7%	0.140
0.00999975	250.405	call funct:	282	call gradient:	28	avoid call:	3105	91.7%	0.150
0.00000000	252.000	call funct:	151	call gradient:	15	avoid call:	1663	91.7%	0.150
0.00999975	253.553	call funct:	171	call gradient:	17	avoid call:	1885	91.7%	0.160
0.00999975	253.276	call funct:	191	call gradient:	19	avoid call:	2106	91.7%	0.170
0.02000046	251.232	call funct:	281	call gradient:	28	avoid call:	3104	91.7%	0.190
0.01999950	250.754	call funct:	443	call gradient:	44	avoid call:	4879	91.7%	0.210
0.01000023	251.502	call funct:	171	call gradient:	17	avoid call:	1885	91.7%	0.220
0.00999975	252.829	call funct:	272	call gradient:	27	avoid call:	2994	91.7%	0.230
0.01999998	254.301	call funct:	272	call gradient:	27	avoid call:	2994	91.7%	0.250
0.01000023	255.552	call funct:	262	call gradient:	26	avoid call:	2884	91.7%	0.260
0.00000000	256.075	call funct:	181	call gradient:	18	avoid call:	1996	91.7%	0.260
0.00999975	255.997	call funct:	251	call gradient:	25	avoid call:	2772	91.7%	0.270
0.01999998	255.539	call funct:	292	call gradient:	29	avoid call:	3215	91.7%	0.290
0.01999998	255.123	call funct:	372	call gradient:	37	avoid call:	4103	91.7%	0.310
0.01999998	255.110	call funct:	433	call gradient:	43	avoid call:	4769	91.7%	0.330
0.01999998	255.316	call funct:	493	call gradient:	49	avoid call:	5435	91.7%	0.350
0.01999998	255.524	call funct:	413	call gradient:	41	avoid call:	4547	91.7%	0.370
0.03000021	255.666	call funct:	544	call gradient:	54	avoid call:	5989	91.7%	0.400

### Filtre sur les familles sous H0

Exemple NICOLAS DESCHAMP

```
5   : NP
5   : NM
5   : Effets de nuisances
61  : NTNIV
```

TEMPS UNIT   LRT   NB APPEL FUNCT Famille IP,JM   NB APPEL GRADIENT   APPEL EVITE   NB APPEL EVITE/ APPEL TOTAL   TEMPS CUMULES						
-						
0.50999928	208.862 call funct:	11375 call gradient:	125 avoid call:	0 0.0%	0.510	
0.92000103	204.470 call funct:	13875 call gradient:	125 avoid call:	0 0.0%	1.430	
0.10000038	204.348 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	1.530	
0.09000015	204.215 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	1.620	
0.10000038	204.069 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	1.720	
0.10000038	203.910 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	1.820	
0.09000015	203.739 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	1.910	
0.10000038	203.555 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	2.010	
0.09000015	203.361 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	2.100	
0.12999916	203.155 call funct:	1998 call gradient:	18 avoid call:	0 0.0%	2.230	
0.09000015	202.941 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	2.320	
0.13000107	202.719 call funct:	1998 call gradient:	18 avoid call:	0 0.0%	2.450	
0.08999825	202.491 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	2.540	
0.09000015	202.266 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	2.630	
0.12000084	202.028 call funct:	1887 call gradient:	17 avoid call:	0 0.0%	2.750	
0.10000038	201.798 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	2.850	
0.12000084	201.571 call funct:	1887 call gradient:	17 avoid call:	0 0.0%	2.970	
0.07999992	201.351 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	3.050	
0.09000015	201.141 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	3.140	
0.09000015	200.941 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	3.230	
0.34000015	200.749 call funct:	5217 call gradient:	47 avoid call:	0 0.0%	3.570	
0.09000015	200.576 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	3.660	
0.10000038	200.418 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	3.760	
0.11999893	200.277 call funct:	1776 call gradient:	16 avoid call:	0 0.0%	3.880	
0.07000160	200.152 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	3.950	
0.10000038	200.043 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	4.050	
0.12000084	199.936 call funct:	1887 call gradient:	17 avoid call:	0 0.0%	4.170	
0.09000015	200.079 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	4.260	
0.10999870	200.292 call funct:	1665 call gradient:	15 avoid call:	0 0.0%	4.370	
0.11000061	200.570 call funct:	1665 call gradient:	15 avoid call:	0 0.0%	4.480	
0.14999962	200.964 call funct:	2109 call gradient:	19 avoid call:	0 0.0%	4.630	
0.07999992	201.033 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	4.710	
0.05999947	201.115 call funct:	777 call gradient:	7 avoid call:	0 0.0%	4.770	
0.06999969	201.211 call funct:	999 call gradient:	9 avoid call:	0 0.0%	4.840	
0.09000015	201.320 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	4.930	
0.07999992	201.444 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	5.010	
0.05999947	201.583 call funct:	888 call gradient:	8 avoid call:	0 0.0%	5.070	
0.07999992	201.736 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	5.150	
0.12000084	201.901 call funct:	1776 call gradient:	16 avoid call:	0 0.0%	5.270	
0.07999992	202.077 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	5.350	
0.12999916	202.260 call funct:	1887 call gradient:	17 avoid call:	0 0.0%	5.480	
0.22000122	202.445 call funct:	3330 call gradient:	30 avoid call:	0 0.0%	5.700	
0.10000038	202.631 call funct:	1443 call gradient:	13 avoid call:	0 0.0%	5.800	
0.11000061	202.811 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	5.910	
0.09000015	202.983 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	6.000	
0.11999893	203.142 call funct:	1776 call gradient:	16 avoid call:	0 0.0%	6.120	
0.22999954	203.916 call funct:	3552 call gradient:	32 avoid call:	0 0.0%	6.350	
0.10000038	204.053 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	6.450	
0.12999916	204.170 call funct:	1998 call gradient:	18 avoid call:	0 0.0%	6.580	
0.07999992	204.268 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	6.660	
0.11000061	204.347 call funct:	1665 call gradient:	15 avoid call:	0 0.0%	6.770	
0.11000061	204.410 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	6.880	
0.15999985	204.457 call funct:	2331 call gradient:	21 avoid call:	0 0.0%	7.040	
0.09000015	204.491 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	7.130	
0.07999992	204.515 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	7.210	
0.12000084	204.529 call funct:	1776 call gradient:	16 avoid call:	0 0.0%	7.330	
0.09000015	204.536 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	7.420	
0.10999870	204.536 call funct:	1554 call gradient:	14 avoid call:	0 0.0%	7.530	
0.09000015	204.532 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	7.620	
0.07999992	204.523 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	7.700	
0.13999939	204.105 call funct:	2220 call gradient:	20 avoid call:	0 0.0%	7.840	
0.07999992	204.105 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	7.920	
0.09000015	204.104 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	8.010	
0.06999969	204.102 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	8.080	
0.06999969	204.099 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	8.150	
0.06999969	204.096 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	8.220	
0.09000015	204.093 call funct:	1332 call gradient:	12 avoid call:	0 0.0%	8.310	
0.06999969	204.089 call funct:	1110 call gradient:	10 avoid call:	0 0.0%	8.380	
0.07999992	204.085 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	8.460	
0.07999992	204.080 call funct:	1221 call gradient:	11 avoid call:	0 0.0%	8.540	
0.19000053	249.937 call funct:	2990 call gradient:	46 avoid call:	0 0.0%	8.730	
0.35999870	262.708 call funct:	5642 call gradient:	62 avoid call:	0 0.0%	9.090	
0.87000084	204.835 call funct:	14980 call gradient:	140 avoid call:	0 0.0%	9.960	

\* Gradient Optimisé \*

TEMPS UNIT | LRT | NB APPEL FUNCT Famille IP,JM | NB APPEL GRADIENT | APPEL EVITE | NB APPEL EVITE/ APPEL TOTAL | TEMPS CUMULES

**NOTE :**

- -

Les 3 derniers appels sont les tests de nuisance, je n'ai pas encore appliquer cette optimisation dessus.....

### Filtre sur les familles sous $H_0$

- -

Exemple PORC

```
4 : NP
16 : NM
0 : Effets de nuisances
16 : NTNIV (H1)
```

\* pas optimisé \*

TEMPS UNIT | LRT | NB APPEL FUNCT Famille IP,JM | NB APPEL GRADIENT | APPEL EVITE | NB APPEL EVITE/ APPEL TOTAL | TEMPS CUMULES

0.00000000	104.752 call funct:	475 call gradient:	19 avoid call:	0 0.0%	0.000	
0.01999998	100.026 call funct:	1025 call gradient:	25 avoid call:	0 0.0%	0.020	
0.00000000	100.182 call funct:	697 call gradient:	17 avoid call:	0 0.0%	0.020	
0.00999999	100.027 call funct:	615 call gradient:	15 avoid call:	0 0.0%	0.030	
0.01000023	99.836 call funct:	656 call gradient:	16 avoid call:	0 0.0%	0.040	
0.00000000	99.623 call funct:	369 call gradient:	9 avoid call:	0 0.0%	0.040	
0.00999975	98.302 call funct:	574 call gradient:	14 avoid call:	0 0.0%	0.050	
0.01000023	95.634 call funct:	735 call gradient:	18 avoid call:	0 0.0%	0.060	
0.00999975	92.542 call funct:	693 call gradient:	17 avoid call:	0 0.0%	0.070	
0.00000000	89.819 call funct:	694 call gradient:	17 avoid call:	0 0.0%	0.070	
0.00000000	88.151 call funct:	612 call gradient:	15 avoid call:	0 0.0%	0.070	
0.00999975	87.539 call funct:	738 call gradient:	18 avoid call:	0 0.0%	0.080	
0.01000023	85.114 call funct:	613 call gradient:	15 avoid call:	0 0.0%	0.090	
0.00999975	82.337 call funct:	735 call gradient:	18 avoid call:	0 0.0%	0.100	
0.00000000	79.264 call funct:	736 call gradient:	18 avoid call:	0 0.0%	0.100	
0.01000023	79.241 call funct:	736 call gradient:	18 avoid call:	0 0.0%	0.110	
0.00999975	80.986 call funct:	656 call gradient:	16 avoid call:	0 0.0%	0.120	
0.01000023	82.044 call funct:	696 call gradient:	17 avoid call:	0 0.0%	0.130	
0.00000000	84.790 call funct:	696 call gradient:	17 avoid call:	0 0.0%	0.130	
0.00999975	89.367 call funct:	615 call gradient:	15 avoid call:	0 0.0%	0.140	
0.01000023	93.955 call funct:	656 call gradient:	16 avoid call:	0 0.0%	0.150	
0.00999999	97.184 call funct:	615 call gradient:	15 avoid call:	0 0.0%	0.160	
0.00000000	95.365 call funct:	655 call gradient:	16 avoid call:	0 0.0%	0.160	
0.00999999	94.530 call funct:	614 call gradient:	15 avoid call:	0 0.0%	0.170	
0.00999999	95.378 call funct:	820 call gradient:	20 avoid call:	0 0.0%	0.180	
0.00999999	96.179 call funct:	492 call gradient:	12 avoid call:	0 0.0%	0.190	
0.00000000	96.215 call funct:	533 call gradient:	13 avoid call:	0 0.0%	0.190	
0.00999999	96.635 call funct:	410 call gradient:	10 avoid call:	0 0.0%	0.200	
0.00000000	97.462 call funct:	492 call gradient:	12 avoid call:	0 0.0%	0.200	
0.00999999	98.462 call funct:	492 call gradient:	12 avoid call:	0 0.0%	0.210	
0.00999999	99.325 call funct:	533 call gradient:	13 avoid call:	0 0.0%	0.220	
0.00000000	99.863 call funct:	451 call gradient:	11 avoid call:	0 0.0%	0.220	
0.00999999	100.522 call funct:	451 call gradient:	11 avoid call:	0 0.0%	0.230	
0.00000000	101.187 call funct:	533 call gradient:	13 avoid call:	0 0.0%	0.230	
0.00999999	101.664 call funct:	533 call gradient:	13 avoid call:	0 0.0%	0.240	

\* Gradient Optimisé \*

TEMPS UNIT | LRT | NB APPEL FUNCT Famille IP,JM | NB APPEL GRADIENT | APPEL EVITE | NB APPEL EVITE/ APPEL TOTAL | TEMPS CUMULES

0.00999999	104.752 call funct:	135 call gradient:	19 avoid call:	339 71.5%	0.010
0.00000000	100.026 call funct:	231 call gradient:	24 avoid call:	753 76.5%	0.010
0.00000000	100.182 call funct:	163 call gradient:	17 avoid call:	533 76.5%	0.010
0.00000000	100.027 call funct:	144 call gradient:	15 avoid call:	470 76.5%	0.010
0.00999999	99.836 call funct:	154 call gradient:	16 avoid call:	502 76.5%	0.020
0.00000000	99.623 call funct:	86 call gradient:	9 avoid call:	282 76.5%	0.020
0.00000000	98.302 call funct:	134 call gradient:	14 avoid call:	439 76.5%	0.020
0.00000000	95.634 call funct:	172 call gradient:	18 avoid call:	562 76.5%	0.020
0.00999999	92.542 call funct:	162 call gradient:	17 avoid call:	530 76.5%	0.030
0.00000000	89.819 call funct:	162 call gradient:	17 avoid call:	531 76.5%	0.030
0.00000000	88.151 call funct:	143 call gradient:	15 avoid call:	468 76.5%	0.030
0.00000000	87.539 call funct:	173 call gradient:	18 avoid call:	564 76.5%	0.030
0.01000023	85.114 call funct:	143 call gradient:	15 avoid call:	469 76.5%	0.040
0.00000000	82.337 call funct:	172 call gradient:	18 avoid call:	562 76.5%	0.040
0.00000000	79.264 call funct:	172 call gradient:	18 avoid call:	563 76.5%	0.040
0.00000000	79.241 call funct:	172 call gradient:	18 avoid call:	563 76.5%	0.040
0.00999975	80.986 call funct:	154 call gradient:	16 avoid call:	502 76.5%	0.050
0.00000000	82.044 call funct:	163 call gradient:	17 avoid call:	532 76.5%	0.050
0.00000000	84.790 call funct:	163 call gradient:	17 avoid call:	532 76.5%	0.050
0.00000000	89.367 call funct:	144 call gradient:	15 avoid call:	470 76.5%	0.050
0.00000000	93.955 call funct:	154 call gradient:	16 avoid call:	502 76.5%	0.050
0.00000000	97.184 call funct:	144 call gradient:	15 avoid call:	470 76.5%	0.050
0.00000000	95.365 call funct:	153 call gradient:	16 avoid call:	501 76.5%	0.050
0.00000000	94.530 call funct:	144 call gradient:	15 avoid call:	469 76.5%	0.050
0.00000000	95.378 call funct:	192 call gradient:	20 avoid call:	627 76.5%	0.050
0.00999975	96.179 call funct:	115 call gradient:	12 avoid call:	376 76.5%	0.060
0.00000000	96.215 call funct:	125 call gradient:	13 avoid call:	407 76.5%	0.060
0.00000000	96.635 call funct:	96 call gradient:	10 avoid call:	313 76.5%	0.060
0.00000000	97.462 call funct:	115 call gradient:	12 avoid call:	376 76.5%	0.060
0.00000000	98.462 call funct:	115 call gradient:	12 avoid call:	376 76.5%	0.060
0.01000023	99.325 call funct:	125 call gradient:	13 avoid call:	407 76.5%	0.070
0.00000000	99.863 call funct:	105 call gradient:	11 avoid call:	345 76.5%	0.070
0.00000000	100.522 call funct:	105 call gradient:	11 avoid call:	345 76.5%	0.070
0.00000000	101.187 call funct:	125 call gradient:	13 avoid call:	407 76.5%	0.070
0.00000000	101.664 call funct:	125 call gradient:	13 avoid call:	407 76.5%	0.070

Filtre sur les famille sous H0

IP	JM	KD1	KD2	FILTRE
1	1	1	28	T F F F T T F F T F F F
1	2	29	32	T F F F T T F F T F F F
1	3	33	47	T F F F T T F F T F F F
1	4	48	58	T F F F T T F F T F F F
2	5	59	72	F T F F T F T F F F F F
2	6	73	76	F T F F T F T F F F F F
2	7	77	90	F T F F T F T F F F F F
2	8	91	99	F T F F T F T F F F F F
3	9	100	123	F T F F T F F T F F F
3	10	124	150	F F T F T F F T F F T F
3	11	151	160	F F T F T F F T F F F F
3	12	161	174	F F T F T F F T F F F F
3	13	175	182	F F T F T F F T F F F F
4	14	183	197	F F F T T F F F F F F F
4	15	198	212	F F F T T F F F F F F F
4	16	213	236	F F F T T F F F F F F T